

# DECOMPOSING DISJUNCTION

## THE MORPHOSEMANTIC MAKEUP OF XOR

---

Moreno Mitrović

October 12, 2016

University of Saarland

# INTRODUCTION

---

## WHAT THIS TALK IS ABOUT, IN A NUTSHELL

- This talk is about a seemingly **illogical** fact of language that has gone unnoticed:

**or+and** John **or+and** Mary = **either** John **or** Mary

- Two logically opposite particles build a complex particle that expresses strong disjunction (XOR).
- A sketch of these particles ...

# INTRODUCTION

---

SUPERPARTICLES: TWO LOGICAL ATOMS

## SUPERPARTICLES: TWO LOGICAL CLASSES IN JAPANESE

The  $\mu$ -series (*mo*)

The  $\kappa$ -series (*ka*)

## The $\mu$ -series (*mo*)

- a. Bill **mo** Mary **mo**  
B  $\mu$  M  $\mu$   
'(both) Bill and Mary.'

## The $\kappa$ -series (*ka*)

- a. Bill **ka** Mary **ka**  
B  $\kappa$  M  $\kappa$   
'(either) Bill or Mary.'

## The $\mu$ -series (*mo*)

- a. Bill **mo** Mary **mo**  
B  $\mu$  M  $\mu$   
'(both) Bill **and** Mary.'
- b. Mary **mo**  
M  $\mu$   
'**also** Mary'

## The $\kappa$ -series (*ka*)

- a. Bill **ka** Mary **ka**  
B  $\kappa$  M  $\kappa$   
'(either) Bill **or** Mary.'
- b. wakaru **ka**  
understand  $\kappa$   
'Do you understand?'

## The $\mu$ -series (*mo*)

- a. Bill **mo** Mary **mo**  
B  $\mu$  M  $\mu$   
'(both) Bill **and** Mary.'
- b. Mary **mo**  
M  $\mu$   
'**also** Mary'
- c. dare **mo**  
who  $\mu$   
'**every-/any-one**'

## The $\kappa$ -series (*ka*)

- a. Bill **ka** Mary **ka**  
B  $\kappa$  M  $\kappa$   
'(either) Bill **or** Mary.'
- b. wakaru **ka**  
understand  $\kappa$   
'Do you understand?'
- c. dare **ka**  
who  $\kappa$   
'**someone**'



- There seems to exist a **disharmonic mapping** between the **morphologically complex particle clusters** and the **logically/semantically simple meanings** they contribute.

- There seems to exist a **disharmonic mapping** between the **morphologically complex particle clusters** and the **logically/semantically simple meanings** they contribute.
- How can we reconcile this? By assuming compositionality **below the word level**.

- There seems to exist a **disharmonic mapping** between the **morphologically complex particle clusters** and the **logically/semantically simple meanings** they contribute.
- How can we reconcile this? By assuming compositionality **below the word level**.
- This is in line with the larger research programme:

- There seems to exist a **disharmonic mapping** between the **morphologically complex particle clusters** and the **logically/semantically simple meanings** they contribute.
- How can we reconcile this? By assuming compositionality **below the word level**.
- This is in line with the larger research programme:

### The Morphosemantic Principle

"Compositional analysis cannot stop at word-level." (Szabolcsi, 2010, 189, ex. 1)

# INTRODUCTION

---

DISJUNCTIONS, IMPLICATURES,  
ALTERNATIVES

## AMBIGUOUS 'OR' IN ENGLISH

- In English, 'or' is always **ambiguous** between two *implicated meanings*.
  - a. Either it carries an **IGNORANCE implicature**,
  - b. or it carries a **SCALAR implicature**.

## AMBIGUOUS 'OR' IN ENGLISH

- In English, 'or' is always **ambiguous** between two *implicated meanings*.
  - a. Either it carries an **IGNORANCE implicature**,
  - b. or it carries a **SCALAR implicature**.

(1)  $\llbracket \text{Mary saw John or Bill.} \rrbracket = j \vee b$

## AMBIGUOUS 'OR' IN ENGLISH

- In English, 'or' is always **ambiguous** between two *implicated meanings*.
  - a. Either it carries an **IGNORANCE implicature**,
  - b. or it carries a **SCALAR implicature**.

(1)  $\llbracket \text{Mary saw John or Bill.} \rrbracket = j \vee b$

a. (1)  $\rightsquigarrow \diamond[j] \wedge \diamond[b] \wedge \diamond[j \vee b] \wedge \diamond[j \wedge b]$

"The speaker **doesn't know** whether Mary saw **John** and the speaker **doesn't know** whether Mary saw **Bill** and the speaker **doesn't know** whether Mary saw **John and Bill**."



## AMBIGUOUS 'OR' IN ENGLISH

- In English, 'or' is always **ambiguous** between two *implicated meanings*.
  - a. Either it carries an **IGNORANCE implicature**,
  - b. or it carries a **SCALAR implicature**.

(1)  $\llbracket \text{Mary saw John or Bill.} \rrbracket = j \vee b$

a. (1)  $\rightsquigarrow \diamond[j] \wedge \diamond[b] \wedge \diamond[j \vee b] \wedge \diamond[j \wedge b]$

"The speaker **doesn't know** whether Mary saw **John** and the speaker **doesn't know** whether Mary saw **Bill** and the speaker **doesn't know** whether Mary saw **John and Bill**."

b. (1)  $\rightsquigarrow [j \vee b] \wedge \neg[j \wedge b]$

"Mary saw **John or Bill**, but **not both**."

## FORMALISING ALTERNATIVES & THEIR PRUNING

*j v b*

## FORMALISING ALTERNATIVES & THEIR PRUNING

$j \vee b$

← assertion

## FORMALISING ALTERNATIVES & THEIR PRUNING

$j \vee b$

← assertion

$\mathfrak{A}$

## FORMALISING ALTERNATIVES & THEIR PRUNING

$j \vee b$

← assertion

$\mathcal{A}$

$j \wedge b$

## FORMALISING ALTERNATIVES & THEIR PRUNING

$j \vee b$

← assertion

$\mathcal{A}$

$j \wedge b$

←  $\sigma$ -alts

## FORMALISING ALTERNATIVES & THEIR PRUNING

$j \vee b$

$\alpha$

$j \wedge b$

← assertion

←  $\sigma$ -alts

## FORMALISING ALTERNATIVES & THEIR PRUNING

$j$



$b$

← assertion

←  $\sigma$ -alts



## FORMALISING ALTERNATIVES & THEIR PRUNING

$j$



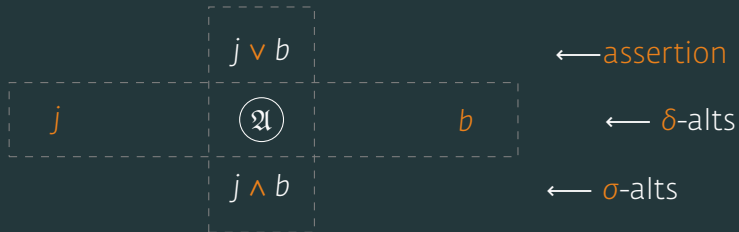
$b$

← assertion

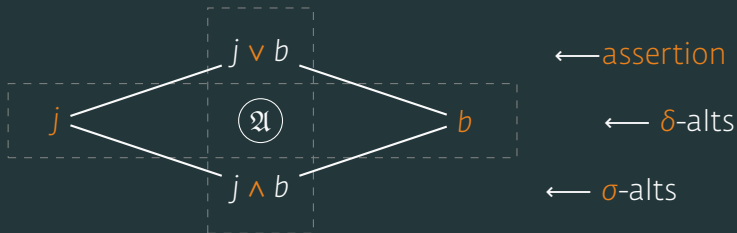
←  $\delta$ -alts

←  $\sigma$ -alts

## FORMALISING ALTERNATIVES & THEIR PRUNING

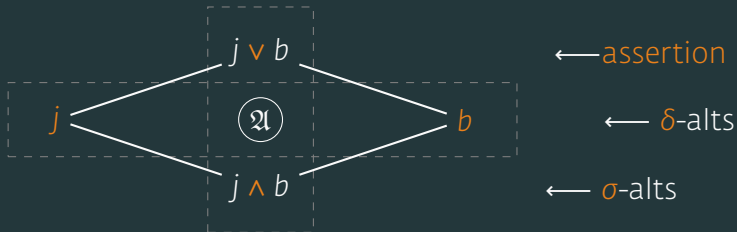


## FORMALISING ALTERNATIVES & THEIR PRUNING



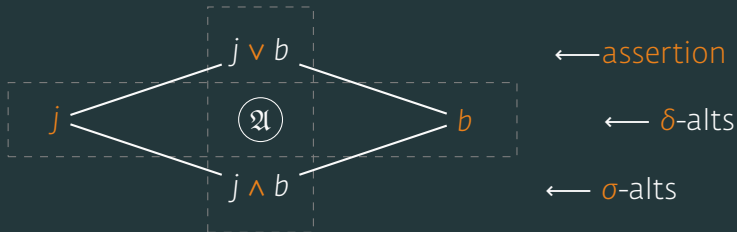
- ∴ There two kinds of alternatives: **subdomain** ( $\delta$ ) and **scalar** ( $\sigma$ ) ones.
- The choice between which ones are relevant is made in syntax using a covert exhaustification operator akin to a silent '**only**' –  $\text{æ}$ .

## FORMALISING ALTERNATIVES & THEIR PRUNING



- ∴ There two kinds of alternatives: **subdomain** ( $\delta$ ) and **scalar** ( $\sigma$ ) ones.

## FORMALISING ALTERNATIVES & THEIR PRUNING



- ∴ There two kinds of alternatives: **subdomain** ( $\delta$ ) and **scalar** ( $\sigma$ ) ones.
- The choice between which ones are relevant is made in syntax using a covert exhaustification operator akin to a silent '**only**' –  $\text{⊔}$ .

## THE SILENT EXHAUSTIFIER

- The operator  $\mathfrak{X}$  is a silent variant of the adverb 'only'.
- What does it mean?

$$(2) \quad \mathfrak{X}(p) = p \wedge \forall q \in \mathfrak{A}(p) \left[ [p \text{ } \# \text{ } q] \rightarrow \neg q \right]$$

- This LF is read as: **the assertion,  $p$ , is true and any non-entailed alternative to the assertion,  $q$  an alternative, is false.**

- Consider the enriched F-associated meanings:

(3) Mary saw **John**.

## THE SILENT EXHAUSTIFIER: A SKETCH OF APPLICATION

- Consider the enriched F-associated meanings:

(3) Mary saw **John**. ..... NO ALTS TRIGGERED



## THE SILENT EXHAUSTIFIER: A SKETCH OF APPLICATION

- Consider the enriched F-associated meanings:

- (3) Mary saw **John**. ..... NO ALTS TRIGGERED
  - a. Mary saw **only John**.

## THE SILENT EXHAUSTIFIER: A SKETCH OF APPLICATION

- Consider the enriched F-associated meanings:

- (3) Mary saw **John**. ..... NO ALTS TRIGGERED
- a. Mary saw **only John**. .....  $\delta$ -ALTS TRIGGERED!
- b. Mary saw **JOHN**.

## THE SILENT EXHAUSTIFIER: A SKETCH OF APPLICATION

- Consider the enriched F-associated meanings:

- (3) Mary saw **John**. ..... NO ALTS TRIGGERED
- a. Mary saw **only John**. .....  $\delta$ -ALTS TRIGGERED!
- b. Mary saw **J O H N**. .....  $\delta$ -ALTS TRIGGERED!

## THE SILENT EXHAUSTIFIER: A SKETCH OF APPLICATION

- Consider the enriched F-associated meanings:

- (3) Mary saw **John**. ..... NO ALTS TRIGGERED
- a. Mary saw **only John**. .....  $\delta$ -ALTS TRIGGERED!
- b. Mary saw **J O H N**. .....  $\delta$ -ALTS TRIGGERED!

- We take (3b) to be rather analogous to (3a):

# THE SILENT EXHAUSTIFIER: A SKETCH OF APPLICATION

- Consider the enriched F-associated meanings:

- (3) **Mary saw John.** ..... NO ALTS TRIGGERED
- a. **Mary saw only John.** .....  $\delta$ -ALTS TRIGGERED!
- b. **Mary saw JOHN.** .....  $\delta$ -ALTS TRIGGERED!

- We take (3b) to be rather analogous to (3a):

- (4)  $\left[ \mathfrak{X}_{[\alpha:\delta]} \left[ \text{Mary saw } \text{JOHN}_\delta \right] \right]$

- Exhaustification need not result in intonational marking.  
(SKETCH)
- Some words have constantly active alternatives  
(inversely, Focus may activate otherwise passive alternatives).
- This activity is syntactically visible by a presence of (one of the)  $[\sigma, \delta]$  features.
- A class of these constantly- $\mathfrak{A}$ -active words includes **indefinites**, **disjunctions**, and a special class **conjunctions**, a.o.
- Crucially, our  $\mu$  and  $\kappa$  markers are such words.
- When alternatives are active, **exhaustification is obligatory**.

- Turning back to the English facts: disjunction is inherently implicative may yield
  - an **ignorance implicature**, or
  - a **scalar implicature** (SI).

(5) **Mary saw John or (Mary saw) Bill.**

- Turning back to the English facts: disjunction is inherently implicative may yield
  - an **ignorance implicature**, or
  - a **scalar implicature** (SI).

(5) **Mary saw John or (Mary saw) Bill.**

- We focus on the SI.
- There are two ways of calculating the SI and deriving the exclusive component:
  - locally
  - globally



## (A) GLOBAL CALCULATION

- GLOBAL CALCULATION of the exclusive component via  $\mathfrak{X}_{[\sigma\lambda]}$

i. Syntactic structure (simplified):



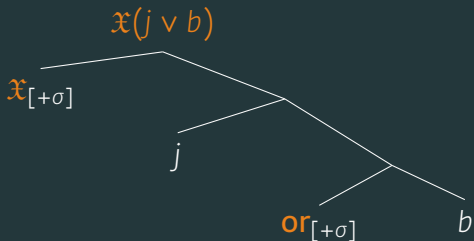
ii. Logical form:

$$\mathfrak{X}_{[\sigma\lambda]}(j \vee b) = [j \vee b] \wedge \neg[j \wedge b]$$

## (A) GLOBAL CALCULATION

- GLOBAL CALCULATION of the exclusive component via  $\mathfrak{X}_{[\sigma\lambda]}$

i. Syntactic structure (simplified):



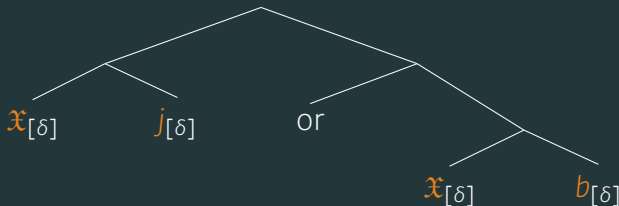
ii. Logical form:

$$\mathfrak{X}_{[\sigma\lambda]}(j \vee b) = [j \vee b] \wedge \neg[j \wedge b]$$

## (B) LOCAL CALCULATION

- LOCAL CALCULATION of the exclusive component via  $\mathfrak{X}_{[\delta\alpha]}$

i. Syntactic structure (simplified):



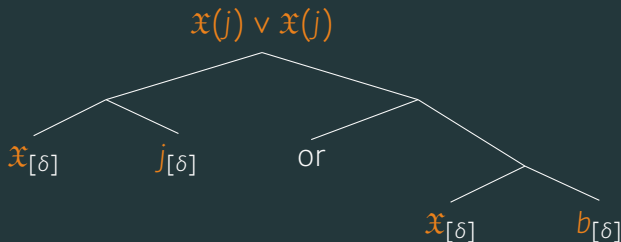
ii. Logical form:

$$\mathfrak{X}_{[\delta\alpha]}(j \vee b) = \mathfrak{X}(j) \vee \mathfrak{X}(b) \vdash \neg[j \wedge b]$$

## (B) LOCAL CALCULATION

- LOCAL CALCULATION of the exclusive component via  $\mathfrak{x}_{[\delta\alpha]}$

i. Syntactic structure (simplified):



ii. Logical form:

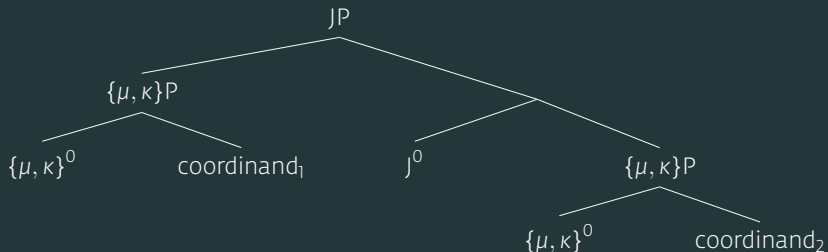
$$\mathfrak{x}_{[\delta\alpha]}(j \vee b) = \mathfrak{x}(j) \vee \mathfrak{x}(b) \vdash \neg[j \wedge b]$$

# THE MEANINGS OF SUPERPARTICLES

---

- We now propose two lexical entries for the two superparticles  $\mu$  and  $\kappa$ , and the Junction head which forms coordination.
- Syntactically, we take the view that conjunction and disjunction are both part of a **junction structure** (JP) with an abstract Junction head.

- We now propose two lexical entries for the two superparticles  $\mu$  and  $\kappa$ , and the Junction head which forms coordination.
- Syntactically, we take the view that conjunction and disjunction are both part of a **junction structure** (JP) with an abstract Junction head.



- We assume that  $\mu$ ,  $\kappa$ , and  $J$  have the following meanings (very generally, see Mitrović 2014 for details):

$\mu$     •  $\llbracket \mu \rrbracket(p) = \mathfrak{X}(\mathfrak{X}(p)) = \neg \mathfrak{X}p$

$\kappa$  performs inquisitive closure

•  $\llbracket \kappa \rrbracket(p) = p \vee \neg p = \{p, \neg p\}$

$J$



## EVIDENCE & PUZZLE

---

## THE PUZZLING EVIDENCE

- We now turn to the actual problem at hand and present fresh data where both  $\mu$  and  $\kappa$  markers are used to build XOR words.
- We propose and defend two generalisation.

(6) a. GENERALISATION 1

Disjunction markers ( $\kappa$ -class) tend to feature in morphologically more complex expression than the conjunction markers ( $\mu$ -class) do.

b. GENERALISATION 2

Morphologically complex disjunction markers may include the conjunction markers ( $\mu$ -class).

## SO MANY PARTICLES IN SO MANY LANGUAGES

- Evidence from **seven languages** (five language families) supports this:
  - Homeric Greek (†)
  - Hittite (†)
  - Tocharian (†)
  - Slavonic (Ser-Bo-Croatian)
  - NE Caucasian (Avar, Dargi)
- I now turn to buttressing these facts.

# EVIDENCE & PUZZLE

---

## THE CORE DATA

(7) **ē-t(e)** ehremen para soi  
κ-μ keep with self  
'...or [else] to keep with yourself' (Il. T. 148)

(8) **ei-te** boulesthe polemein emin **ei-te** filoi  
κ-μ wish to be at war for myself κ-μ friend  
einai  
be  
'whether you wish to wage war upon us or [else] to be  
our friends'

(Cyrop. 3.2.13.)

- (9) nu-šši     **naššu**                    adanna peškezzi **naš-ma-šši**  
 now-him  $\kappa^2$ -( $\mu$ ) =either eat            give             $\kappa^2$ - $\mu$ -him  
 akuwanna peškezzi  
 drink            give

'He either gives him to eat or he gives him to drink'  
 (KUB 13.4 i 24)

- (10) LU<sub>LU</sub>=**ku**                            GUD=**ku** [UD]U=**ku**     ēšzi  
 human being-( $\kappa$ +) $\mu$  ox-( $\kappa$ )- $\mu$  [she]ep-( $\kappa$ )- $\mu$  be  
 '...whether it be human being, ox or [she]ep.'

(KBo 6.3 iv 53)

- (11) **pe** klošäm nāñi  
 μ ears.DU 1.GEN  
 'also my ears'

(TA 5: 53, b3/A 58b3 in Zimmer 1976, 90)

- (12) ckācar **e-pe** šäm **e-pe**  
 sister κ-μ wife κ-μ  
 '(either) sister or wife'

(TA 428: a4, b2; Carling 2009, 74)

(13) i Mujo i Haso  
μ M     μ H  
'**Both** Mujo **and** Haso.'

(14) i-li Mujo i-li Haso  
μ-κ M     μ-κ H  
'**Either** Mujo **or** Haso.'



- (15) nu-ni umx u sune-la mer.li-či-b b-arg-i-ra,  
 me-ERG key(ABS) self-GEN place-SUP-N N-find-AOR-1  
 amma **ya** pulaw, **ya** 'är'ä he-d-arg-i-ra  
 but κ pilaf(ABS) κ hen(ABS) NEG-PL-find-AOR-1  
 'I found the key at its place, but **neither** the pilaf **nor**  
 the chicken was there.' (van der Berg 2004, 203)

- (16) il.a-la buruš **ra** yurgan **ra** 'änala  
 this-GEN mattress(ABS) μ blanket(ABS) μ pillow(ABS)  
**ra** kas-ili sa⟨r⟩i  
 μ take-GER be.PL  
 '(They) took his mattress, blanket **and** pillow.'

(van der Berg 2004, 199)

- (17) **ya ra** pilaw b-ir-ehe, **ya ra** nerg b-ir-ehe  
 κ μ pilaf(ABS) N-do-FUT.1 κ μ soup(ABS) N-do-FUT.1  
 ('What shall we make for lunch?') 'We'll make (either)  
 pilaf or soup.'  
 (van der Berg 2004, 204)

(18) keto **gi** hve **gi**  
cat  $\mu$  (J) dog  $\mu$   
'cat and dog'

(Avar; Ramazanov, p.c.)

(19) **ya gi** Sasha    **ya gi** Vanya  
 $\kappa$   $\mu$  S            (J)  $\kappa$   $\mu$  V  
'either Sasha or Vanya.'

(Avar; Mukhtareva, p.c.)

EVIDENCE & PUZZLE

---

SUMMA SUMMARUM



---

Homeric    ē    te       ø    (ē    te)

---

Homeric	$\bar{e}$	te	∅	( $\bar{e}$ te)
Slavonic	li <sub>[+ε]</sub>	i	∅	li <sub>[+ε]</sub> i

## SUMMA SUMMARUM

Homeric	<b>ē</b>	<b>te</b>	∅	<b>(ē te)</b>
Slavonic	<b>li<sub>[+ε]</sub></b>	<b>i</b>	∅	<b>li<sub>[+ε]</sub> i</b>
Hittite	<b>naš</b>	<b>(ma)</b>	∅	<b>naš ma</b>



# SUMMA SUMMARUM

Homeric	ē	te	∅	(ē	te)
Slavonic	li <sub>[+ε]</sub>	i	∅	li <sub>[+ε]</sub>	i
Hittite	naš	(ma)	∅	naš	ma
Tocharian	e	pe	∅	e	pe

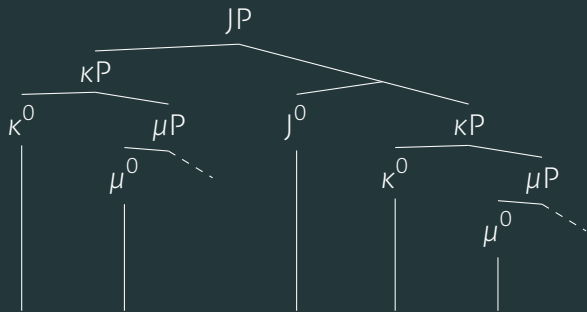
# SUMMA SUMMARUM

Homeric	ē	te	∅	(ē	te)
Slavonic	li <sub>[+ε]</sub>	i	∅	li <sub>[+ε]</sub>	i
Hittite	naš	(ma)	∅	naš	ma
Tocharian	e	pe	∅	e	pe
Dargi	ya	ra	∅	ya	ra

# SUMMA SUMMARUM

Homeric	ē	te	∅	(ē	te)
Slavonic	li <sub>[+ε]</sub>	i	∅	li <sub>[+ε]</sub>	i
Hittite	naš	(ma)	∅	naš	ma
Tocharian	e	pe	∅	e	pe
Dargi	ya	ra	∅	ya	ra

# SUMMA SUMMARUM



Homeric	$\bar{e}$	te	$\emptyset$	( $\bar{e}$	te)
Slavonic	li <sub>[+ε]</sub>	i	$\emptyset$	li <sub>[+ε]</sub>	i
Hittite	naš	(ma)	$\emptyset$	naš	ma
Tocharian	e	pe	$\emptyset$	e	pe
Dargi	ya	ra	$\emptyset$	ya	ra

# ANALYSIS: STRUCTURE & CALCULATION

---

# THE STRUCTURE & THE THEOREM THAT THE DATA SUGGEST

$$a. \left[ \underset{JP^+}{\beta}_{[F:K]}^0 \left[ \underset{JP}{\kappa}_{K_1}^0 [\mu_{P_1} \mu_1^0 \quad XP] \left[ J^0 [\kappa_{K_2}^0 [\mu_{P_2} \mu_2^0 \quad YP]] \right] \right] \right]$$

$$b. \sqcup \left( \llbracket J^0 \rrbracket \left( \llbracket \kappa_1^0 \rrbracket \left( \llbracket \mu_1^0 \rrbracket \left( \llbracket XP \rrbracket \right) \right) \right) \left( \llbracket \kappa_2^0 \rrbracket \left( \llbracket \mu_2^0 \rrbracket \left( \llbracket YP \rrbracket \right) \right) \right) \right)$$

$$c. \text{ THEOREM. } (b) \vdash \llbracket XP \rrbracket \vee \llbracket YP \rrbracket \wedge \neg(\llbracket XP \rrbracket \wedge \llbracket YP \rrbracket)$$

# ANALYSIS: STRUCTURE & CALCULATION

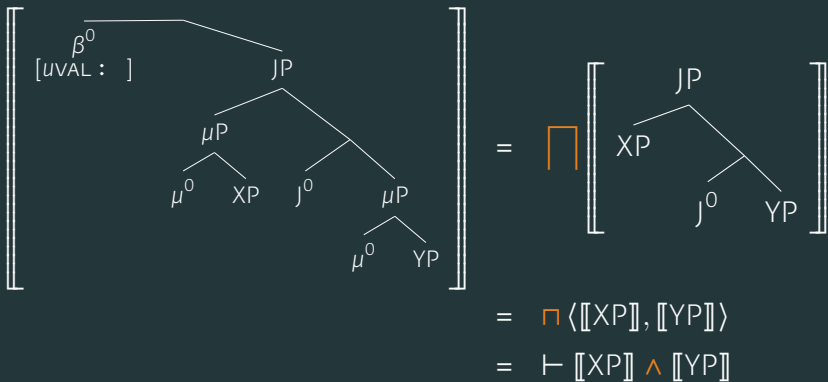
---

PREJACENT MEANING

## DETERMINING THE PREJACENT: SIMPLEX $\mu$ -CONTEXTS

- We assume the prejacents is determined at  $JP^+$  level, by virtue of minimality alone. (cf. Chierchia 2013)

(20) Syntactically rooted MEET:

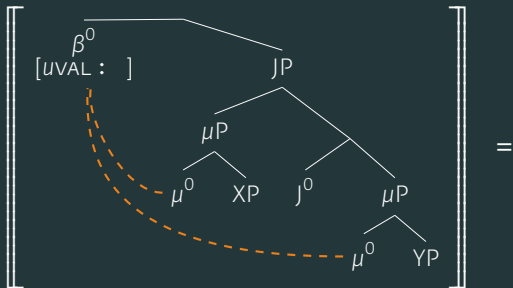




## DETERMINING THE PREJACENT: SIMPLEX $\mu$ -CONTEXTS

- We assume the prejacents is determined at  $JP^+$  level, **by virtue of minimality alone**. (cf. Chierchia 2013)

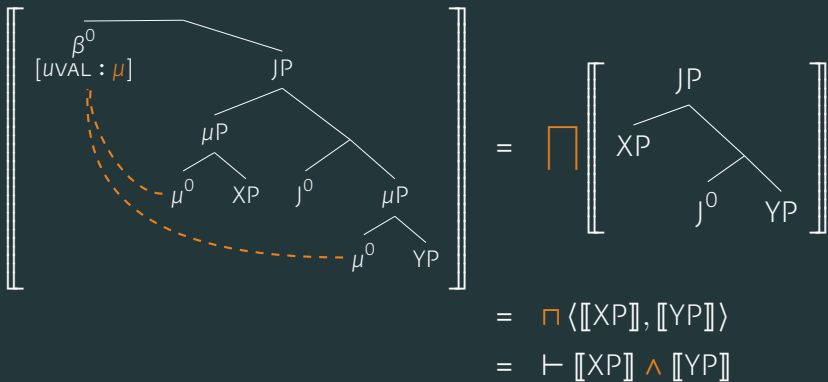
(20) Syntactically rooted MEET:



## DETERMINING THE PREJACENT: SIMPLEX $\mu$ -CONTEXTS

- We assume the prejacents is determined at  $JP^+$  level, by virtue of minimality alone. (cf. Chierchia 2013)

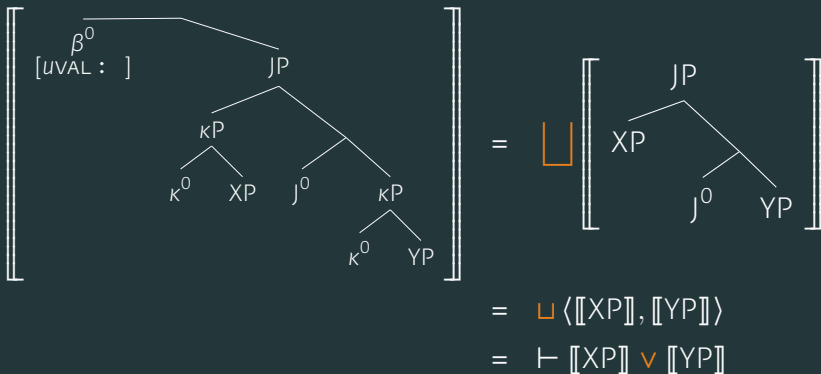
(20) Syntactically rooted MEET:



## DETERMINING THE PREJACENT: SIMPLEX K-CONTEXTS

- We assume the prejacent is determined at  $JP^+$  level, by virtue of minimality alone. (cf. Chierchia 2013)

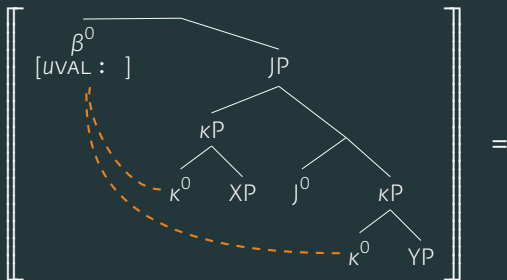
(21) Syntactically rooted JOIN:



## DETERMINING THE PREJACENT: SIMPLEX K-CONTEXTS

- We assume the prejacents is determined at  $JP^+$  level, **by virtue of minimality alone**. (cf. Chierchia 2013)

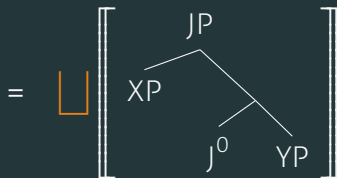
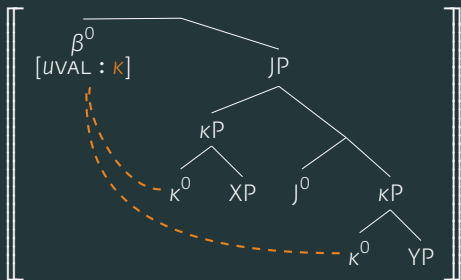
(21) Syntactically rooted JOIN:



## DETERMINING THE PREJACENT: SIMPLEX $\kappa$ -CONTEXTS

- We assume the prejacents is determined at  $JP^+$  level, by virtue of minimality alone. (cf. Chierchia 2013)

(21) Syntactically rooted JOIN:



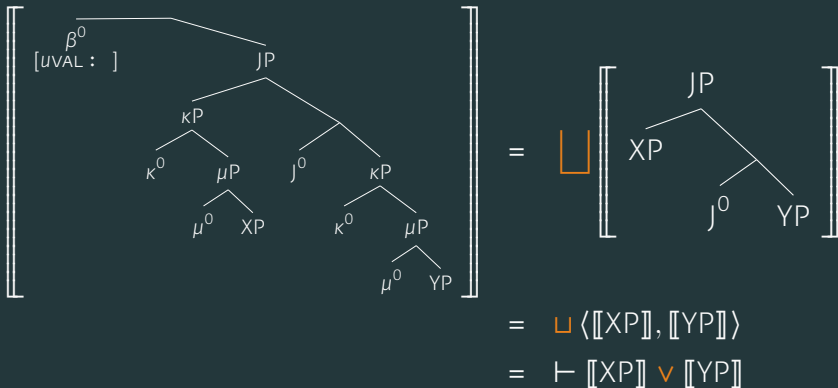
$$= \sqcup \langle \llbracket XP \rrbracket, \llbracket YP \rrbracket \rangle$$

$$= \vdash \llbracket XP \rrbracket \vee \llbracket YP \rrbracket$$

## DETERMINING THE PREJACENT: COMPLEX $\kappa + \mu$ -CONTEXTS

- Let  $\llbracket \text{JP}_{\kappa+\mu}^+ \rrbracket = \bigcap \{ \text{PREJACENT}, \text{ASSERTION/IMPLICATURE} \}$
- $\beta$ -VALUATION determines primary meaning/prejacent.

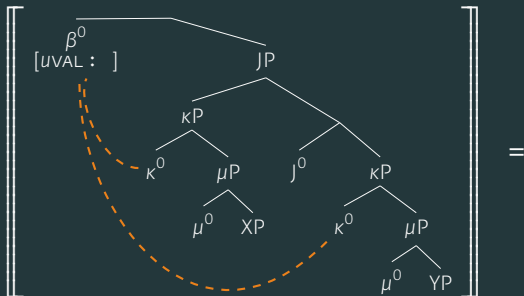
(22) Syntactic competition for **valuation**:



## DETERMINING THE PREJACENT: COMPLEX $\kappa + \mu$ -CONTEXTS

- Let  $\llbracket \text{JP}_{\kappa+\mu}^+ \rrbracket = \bigcap \{ \text{PREJACENT}, \text{ASSERTION/IMPLICATURE} \}$
- $\beta$ -VALUATION determines primary meaning/prejacent.

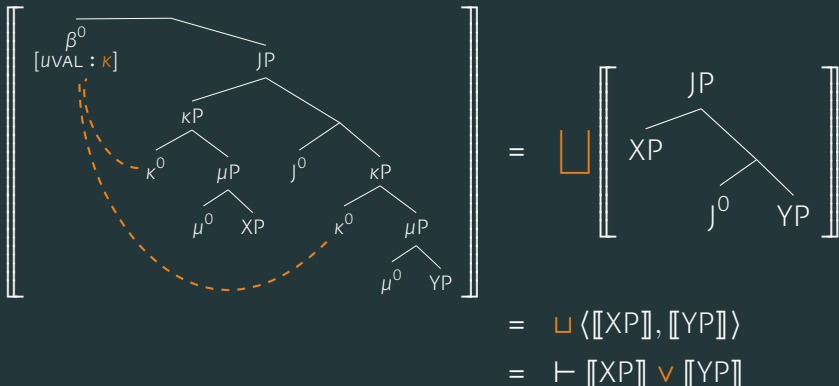
(22) Syntactic competition for **valuation**:



## DETERMINING THE PREJACENT: COMPLEX $\kappa + \mu$ -CONTEXTS

- Let  $\llbracket \text{JP}_{\kappa+\mu}^+ \rrbracket = \bigcap \{ \text{PREJACENT}, \text{ASSERTION/IMPLICATURE} \}$
- $\beta$ -VALUATION determines primary meaning/prejacent.

(22) Syntactic competition for **valuation**:



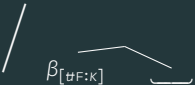


## AN ALLOSEMIC VIEW OF JUNCTION MEANING

- We derived a technical apparatus which deliver the allosemy J.
- We take the necessary configuration for a singly cyclical domain of spell-out to be constrained to a maximal projection, namely JP to the root of which  $\beta$  attaches.

(23) For a pair of coordinands (juncts) XP and YP denoting  $\varphi$  and  $\psi$ , respectively, the Boolean value of  $[[JP [ J^0 XP [ YP ] ]]$  to be structurally conditioned:

a.  $[[JP]] \Leftrightarrow \varphi \wedge \psi$  / 

b.  $[[JP]] \Leftrightarrow \varphi \vee \psi$  / 

## NAVIGATION

Introduction

Superparticles: two logical atoms

Disjunctions, implicatures, alternatives

The meanings of superparticles

Evidence & puzzle

The core data

Summa summarum

Analysis: structure & calculation

Prejacent meaning

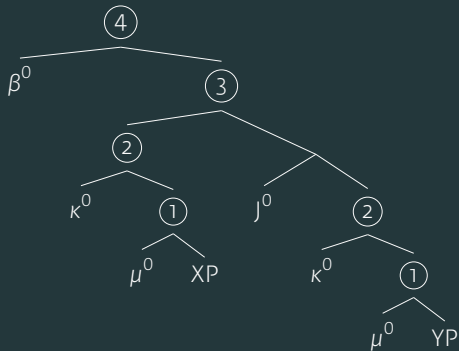
Generating alternatives

# ANALYSIS: STRUCTURE & CALCULATION

---

GENERATING ALTERNATIVES

## THE COMPOSITION



- ①  $[[\mu P]]$  as FA of  $[[\mu^0]]$  and its argument (coordinand)
- ②  $[[kP]]$  as FA of  $[[k^0]]$  and  $[[\mu P]]$
- ③  $[[JP]]$  as tuple-forming FA of  $[[J^0]]$  and two  $[[kP]]$ s (structural coordinands)
- ④  $[[JP^+]]$  as FA of  $[[\beta^0]]$  and  $[[JP]]$

## EXCURSUS: THE $\heartsuit$ -PROCEDURE

- Our alternative set will grow widely.
- We therefore require a system(at)ic procedure that will **prevent inconsistent alternative (sub)sets**.
- The procedure we appeal to is that of **Innocent Exclusion** ( $\heartsuit$ )

$$(24) \quad \mathfrak{X}(\mathfrak{A}_{\langle\langle s,t \rangle, t \rangle})(p)(w) \Leftrightarrow p(w) \wedge \forall q [q \in \heartsuit(p, \mathfrak{A}) \rightarrow \neg q(w)]$$

(Fox, 2007, 26)

## (25) HURFORD'S CONSTRAINT (HC)

Neither of the disjuncts should entail the other, or each other.

a. a disjunction of the form  $X_1 \vee X_2$  is odd if  $X_1$  entails  $X_2$ , or vice versa (Katzir and Singh, 2013, 202)

b. 
$$p \vee q = \begin{cases} \perp & \text{if } p \vdash q \text{ or } q \vdash p \\ \neg\perp & \text{otherwise} \end{cases}$$

- We take HC-violating alternatives to be  $\heartsuit$ -excludable.

## STEP 1

- The meaning of  $\mu P$

(26) a. First layer of exhaustification:

$$\begin{aligned}\mathfrak{x}(p)(\{p\}) &= p \wedge \neg p \\ &\vdash \perp\end{aligned}$$

b. Second layer of exhaustification:

$$\begin{aligned}\mathfrak{x}(p)(\{\mathfrak{x}(p)\}) &= p \wedge \neg \mathfrak{x}(p) \\ &\not\vdash \perp\end{aligned}$$

- For details and further arguments for iterativity of  $\mathfrak{x}$ , see Sauerland 2004, Fox 2007 and Mitrović and Sauerland 2014, *inter. al.*

- The meaning of  $\kappa P$  as saturated by  $\mu P$

(27) Composing  $\kappa P$ :

$$\begin{aligned}
 \llbracket \kappa P \rrbracket &= \llbracket \kappa^0 \rrbracket(\llbracket \mu P \rrbracket) \\
 &= \lambda p[p \vee \neg p]([p \wedge \neg \mathfrak{X}(p)]) \\
 &= [p \wedge \neg \mathfrak{X}(p)] \vee \neg[p \wedge \neg \mathfrak{X}(p)] \\
 \text{(by DEM)} &= [p \wedge \neg \mathfrak{X}(p)] \vee [\neg p \vee \mathfrak{X}(p)] \\
 &= \{[p \wedge \neg \mathfrak{X}(p)], [\neg p \vee \mathfrak{X}(p)]\} \\
 &= \left\{ \{[p \wedge \neg \mathfrak{X}(p)]\}, \{\{\neg p\}, \{\mathfrak{X}(p)\}\} \right\}
 \end{aligned}$$



## STEP 3

- We now pair up the two complex  $\kappa$ Ps:

(28) Composing JP:

$$\begin{aligned} \llbracket JP \rrbracket &= \llbracket J^0 \rrbracket (\llbracket \kappa P_1 \rrbracket) (\llbracket \kappa P_2 \rrbracket) \\ \text{(by Lex. it.)} &= \lambda y \lambda x [x \bullet y] (\llbracket \kappa P_1 \rrbracket) (\llbracket \kappa P_2 \rrbracket) \\ \text{(by FA)} &= \llbracket \kappa P_1 \rrbracket \bullet \llbracket \kappa P_2 \rrbracket \\ &= \langle \llbracket \kappa P_1 \rrbracket, \llbracket \kappa P_2 \rrbracket \rangle \\ &= \langle \llbracket [p \wedge \neg \mathfrak{x}(p)] \vee [\neg p \vee \mathfrak{x}(p)] \rrbracket, \llbracket [q \wedge \neg \mathfrak{x}(q)] \vee [\neg q \vee \mathfrak{x}(q)] \rrbracket \rangle \\ \text{(by AO)} &= \left[ \left\{ \left\{ \llbracket [p \wedge \neg \mathfrak{x}(p)] \rrbracket \right\}, \left\{ \{-p\}, \{\mathfrak{x}(p)\} \right\} \right\} \right] \\ \text{(by AO)} &= \left\langle \left[ \left\{ \left\{ \llbracket [p \wedge \neg \mathfrak{x}(p)] \rrbracket \right\}, \right\} \right], \left[ \left\{ \left\{ \llbracket [q \wedge \neg \mathfrak{x}(q)] \rrbracket \right\}, \right\} \right] \right\rangle \end{aligned}$$

## STEP 4

- The JP-pair is mapped onto disjunction (as per  $\beta$ -valuation)

(29) Composing  $JP^+$ :

$$\begin{aligned} \llbracket JP^+ \rrbracket &= \llbracket \beta^0 \rrbracket (\llbracket JP \rrbracket) \\ \text{(by F-check.)} &= \lambda \langle X, Y \rangle [X \vee Y] (\langle \llbracket KP_1 \rrbracket, \llbracket KP_2 \rrbracket \rangle) \\ \text{(by FA)} &= \langle \llbracket KP_1 \rrbracket, \llbracket KP_2 \rrbracket \rangle \\ &= \llbracket KP_1 \rrbracket \vee \llbracket KP_2 \rrbracket \\ &= \left[ \left\{ \left\{ [p \wedge \neg \mathfrak{x}(p)] \right\}, \right\} \right] \vee \left[ \left\{ \left\{ [q \wedge \neg \mathfrak{x}(q)] \right\}, \right\} \right] \\ &= \left\{ \left\{ \left\{ [p \wedge \neg \mathfrak{x}(p)] \right\}, \right\} \right\}, \left\{ \left\{ \left\{ [q \wedge \neg \mathfrak{x}(q)] \right\}, \right\} \right\} \right\} \\ \text{(by AO)} &= \left\{ \left\{ \left\{ \left\{ \neg p \right\}, \left\{ \mathfrak{x}(p) \right\} \right\} \right\} \right\}, \left\{ \left\{ \left\{ \left\{ \neg q \right\}, \left\{ \mathfrak{x}(q) \right\} \right\} \right\} \right\} \right\} \end{aligned}$$

- Once we 'flatten' the generated alt-set, we end up with the following:

$$\bar{\mathfrak{A}} = \{[p \wedge \neg \mathfrak{x}(p)], [q \wedge \neg \mathfrak{x}(q)], [\neg p], [\neg q], [\mathfrak{x}(p)], [\mathfrak{x}(q)]\}$$

## A CLEANER VERSION OF RESULT

- The alternative set  $\bar{\mathcal{A}}$  is inconsistent.
- We impose the  $\heartsuit$ -function which negates an optimal amount of alternative subsets until consistency obtains.

## A CLEANER VERSION OF RESULT

- The alternative set  $\bar{\mathcal{A}}$  is inconsistent.
- We impose the  $\heartsuit$ -function which negates an optimal amount of alternative subsets until consistency obtains.
- The resulting maximally consistent subsets are:

## A CLEANER VERSION OF RESULT

- The alternative set  $\bar{\mathcal{A}}$  is inconsistent.
- We impose the  $\heartsuit$ -function which negates an optimal amount of alternative subsets until consistency obtains.
- The resulting maximally consistent subsets are:

$$(30) \quad \llbracket \mathbb{J}P^+ \rrbracket = \left\{ \begin{array}{l} [p \wedge \neg \mathfrak{X}(p)], \quad [\neg p \vee \mathfrak{X}(p)], \\ [q \wedge \neg \mathfrak{X}(q)], \quad [\neg q \vee \mathfrak{X}(q)] \end{array} \right\} \dots \vdash \neg \text{CONS}$$

a.  $\{[p \wedge \neg \mathfrak{X}(p)], [q \wedge \neg \mathfrak{X}(q)]\} \dots \dots \dots$ excludable: HC

b.  $\{[\neg p \vee \mathfrak{X}(p)], [\neg q \vee \mathfrak{X}(q)]\}$

i.  $\{\{\neg p\}, \{\neg q\}\} \dots \dots \dots$ excludable:  $\exists C$

ii.  $\{\{\mathfrak{X}(p)\}, \{\mathfrak{X}(q)\}\} \dots \dots \dots \checkmark$

## CONCLUSION

- I tried making sense out of complex morphology for, what seems to be, a rather simple meaning of 'or' or 'v'.
- I have not only shown that five operators (heads) are present in the morphosyntactic expression of exclusive disjunction, but have also presented an analysis of deriving the exclusive component as a computational consequence of five-head/operator composition ( $1 \times J^0, 2 \times \kappa^0, 2 \times \mu^0$ ) and alternative elimination via a  $\heartsuit$ -like procedure (including HC) that handles inconsistencies in the generated alternative set.
- This is a sincere attempt to elucidate the compositional gymnastics of logical units below the word level without compromising either the morphosyntax or the semantics.

**THANK YOU!**



### REFERENCES

---

Carling, G. (2009). *Dictionary and Thesaurus of Tocharian A*, volume 1: A--J. Wiesbaden: Harrassowitz.

Chierchia, G. (2013). *Logic in Grammar: Polarity, Free Choice and Intervention*. Oxford studies in semantics and pragmatics 2. Oxford: Oxford University Press.

Fox, D. (2007). Free choice and scalar implicatures. In Sauerland, U. and Stateva, P., editors, *Presupposition and Implicature in Compositional Semantics*, pages 71--120. London: Palgrave Macmillan.

## REFERENCES II

- Katzir, R. and Singh, R. (2013). Hurford disjunctions: embedded exhaustification and structural economy. *Proceedings of Sinn und Bedeutung* 13, 17:210--216.
- Mitrović, M. (2014). *Morphosyntactic atoms of propositional logic: a philo-logical programme*. PhD thesis, University of Cambridge.
- Mitrović, M. and Sauerland, U. (2014). Decomposing coordination. In Iyer, J. and Kusmer, L., editors, *Proceedings of NELS 44*, volume 2, pages 39--52.
- Sauerland, U. (2004). Scalar implicatures in complex sentences. *Linguistics and Philosophy*, 27:367--391.

Szabolcsi, A. (2010). *Quantification*. Cambridge: Cambridge University Press.

van der Berg, H. (2004). Coordinating constructions in Daghestanian languages. In Haspelmath, M., editor, *Coordinating constructions*, pages 197--226. Amsterdam: John Benjamins.

Zimmer, S. (1976). *Tocharische Bibliographie 1959-1975 mit Nachträgen für den vorhergehenden Zeitraum*. Heidelberg: C. Winter.